



PUBLIC SCHOOL DARBHANGA

SESSION (2020-21)
CLASS-IX
MATHEMATICS
HERON'S FORMULA
REVISION
WORKSHEET(ANSWER KEY)

1. A park, in the shape of a quadrilateral ABCD, has $\angle C = 90^\circ$, $AB = 9$ m, $BC = 12$ m, $CD = 5$ m and $AD = 8$ m. How much area does it occupy?

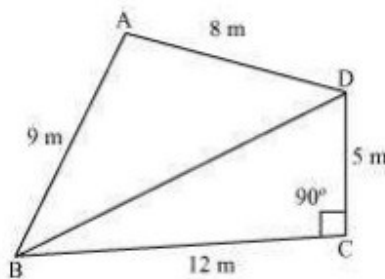
Solution:

First, construct a quadrilateral ABCD and join BD.

We know that

$\angle C = 90^\circ$, $AB = 9$ m, $BC = 12$ m, $CD = 5$ m and $AD = 8$ m

The diagram is:



Now, apply Pythagoras theorem in $\triangle BCD$

$$BD^2 = BC^2 + CD^2$$

$$\Rightarrow BD^2 = 12^2 + 5^2$$

$$\Rightarrow BD^2 = 169$$

$$\Rightarrow BD = 13 \text{ m}$$

Now, the area of $\triangle BCD = (\frac{1}{2} \times 12 \times 5) = 30$

m^2 The semi perimeter of $\triangle ABD$

$$(s) = (\text{perimeter}/2)$$

$$= (8 + 9 + 13)/2 \text{ m}$$

$$= 30/2 \text{ m} = 15 \text{ m}$$

Using Heron's formula,

Area of $\triangle ABD$

$$\sqrt{s(s-a)(s-b)(s-c)}$$

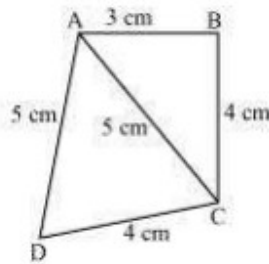
$$= \sqrt{15(15-13)(15-9)(15-8)} \text{ m}^2$$

$$= \sqrt{15 \times 2 \times 6 \times 7} \text{ m}^2$$

$$= 6\sqrt{35} \text{ m}^2 = 35.5 \text{ m}^2 \text{ (approximately)}$$

$$\begin{aligned} \therefore \text{The area of quadrilateral ABCD} &= \text{Area of } \triangle BCD + \text{Area of } \triangle ABD \\ &= 30 \text{ m}^2 + 35.5 \text{ m}^2 = 65.5 \text{ m}^2 \end{aligned}$$

2. Find the area of a quadrilateral ABCD in which AB = 3 cm, BC = 4 cm, CD = 4 cm, DA = 5 cm and AC = 5 cm.



Now, apply Pythagorean theorem in

$$\triangle ABC, AC^2 = AB^2 + BC^2$$

$$\Rightarrow 5^2 = 3^2 + 4^2$$

$$\Rightarrow 25 = 25$$

Thus, it can be concluded that $\triangle ABC$ is a right angled at

B. So, area of $\triangle BCD = (\frac{1}{2} \times 3 \times 4) = 6 \text{ cm}^2$

The semi perimeter of $\triangle ACD$ (s) = (perimeter/2) = $(5 + 5 + 4)/2 \text{ cm} = 14/2 \text{ cm} = 7 \text{ m}$

Now, using Heron's formula,

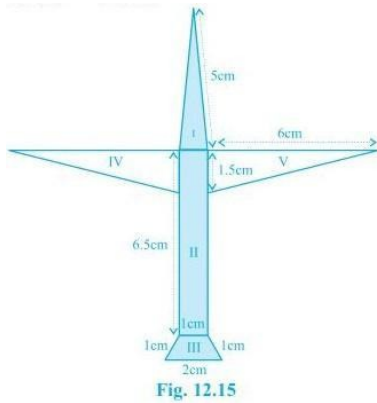
Area of $\triangle ABD$

$$\begin{aligned} &\sqrt{s(s-a)(s-b)(s-c)} \\ &= \left[\sqrt{7(7-5)(7-5)(7-4)} \right] \text{ cm}^2 \\ &= \left(\sqrt{7 \times 2 \times 2 \times 3} \right) \text{ cm}^2 \end{aligned}$$

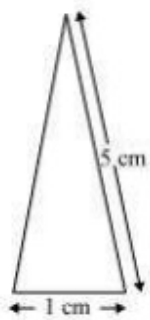
$$= 2\sqrt{21} \text{ cm}^2 = 9.17 \text{ cm}^2 \text{ (approximately)}$$

$$\text{Area of quadrilateral ABCD} = \text{Area of } \triangle ABC + \text{Area of } \triangle ABD = 6 \text{ cm}^2 + 9.17 \text{ cm}^2 = 15.17 \text{ cm}^2$$

3. Radha made a picture of an aeroplane with coloured paper as shown in Fig 12.15. Find the total area of the paper used.



For the triangle I section:



It is an isosceles triangle and the sides are 5 cm, 1 cm and 5 cm

$$\text{Perimeter} = 5 + 5 + 1 = 11 \text{ cm}$$

$$\text{So, semi perimeter} = 11/2 \text{ cm} = 5.5 \text{ cm}$$

Using Heron's formula,

$$\text{Area} = \sqrt{[s (s-a) (s-b) (s-c)]}$$

$$= \sqrt{[5.5(5.5 - 5) (5.5 - 5) (5.5 - 1)] \text{ cm}^2}$$

$$= \sqrt{[5.5 \times 0.5 \times 0.5 \times 4.5] \text{ cm}^2}$$

$$= 0.75\sqrt{11} \text{ cm}^2$$

$$= 0.75 \times 3.317 \text{ cm}^2$$

$$= 2.488\text{cm}^2 \text{ (approx)}$$

For the quadrilateral II section:

This quadrilateral is a rectangle with length and breadth as 6.5 cm and 1 cm respectively.

$$\therefore \text{Area} = 6.5 \times 1 \text{ cm}^2 = 6.5 \text{ cm}^2$$

For the quadrilateral III section:

It is a trapezoid with 2 sides as 1 cm each and the third side as 2 cm.

Area of the trapezoid = Area of the parallelogram + Area of the equilateral triangle

The perpendicular height of the parallelogram will be

$$\left(\sqrt{1^2 - (0.5)^2} \right)$$

$$= 0.86 \text{ cm}$$

And, the area of the equilateral triangle will be $(\sqrt{3}/4 \times a^2) = 0.43$

$$\therefore \text{Area of the trapezoid} = 0.86 + 0.43 = 1.3 \text{ cm}^2 \text{ (approximately).}$$

For triangle IV and V:

These triangles are 2 congruent right angled triangles having the base as 6 cm and height 1.5 cm

$$\text{Area triangles IV and V} = 2 \times (\frac{1}{2} \times 6 \times 1.5) \text{ cm}^2 = 9 \text{ cm}^2$$

$$\text{So, the total area of the paper used} = (2.488 + 6.5 + 1.3 + 9) \text{ cm}^2 = 19.3 \text{ cm}^2$$

4. A triangle and a parallelogram have the same base and the same area. If the sides of the triangle are 26 cm, 28 cm and 30 cm, and the parallelogram stands on the base 28 cm, find the height of the parallelogram.

Given,

It is given that the parallelogram and triangle have equal areas.

The sides of the triangle are given as 26 cm, 28 cm and 30 cm.

So, the perimeter = 26 + 28 + 30 = 84 cm

And its semi perimeter = 84/2 cm = 42 cm

Now, by using Heron's formula, area of the triangle =

$$\sqrt{[s (s-a) (s-b) (s-c)]}$$

$$= \sqrt{[42(42 - 26) (46 - 28) (46 - 30)]} \text{ cm}^2$$

$$= \sqrt{[46 \times 16 \times 14 \times 16]} \text{ cm}^2$$

$$= 336 \text{ cm}^2$$

Now, let the height of parallelogram be h.

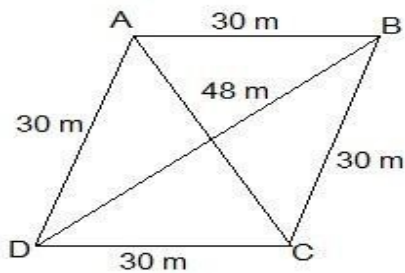
As the area of parallelogram = area of the triangle,

$$28 \text{ cm} \times h = 336 \text{ cm}^2$$

$$\therefore h = 336/28 \text{ cm}$$

So, the height of the parallelogram is 12 cm.

- 5. A rhombus shaped field has green grass for 18 cows to graze. If each side of the rhombus is 30 m and its longer diagonal is 48 m, how much area of grass field will each cow be getting?**



Consider the triangle BCD,

$$\text{Its semi-perimeter} = (48 + 30 + 30)/2 \text{ m} = 54 \text{ m}$$

Using Heron's formula,

Area of the $\triangle BCD =$

$$\sqrt{s(s-a)(s-b)(s-c)}$$

$$\left(\sqrt{54(54-48)(54-30)(54-30)} \right) \text{ m}^2$$

$$\left(\sqrt{54 \times 6 \times 24 \times 24} \right) \text{ m}^2$$

$$= 432 \text{ m}^2$$

$$\therefore \text{Area of field} = 2 \times \text{area of the } \triangle BCD = (2 \times 432) \text{ m}^2 = 864 \text{ m}^2$$

Thus, the area of the grass field that each cow will be getting = $(864/18) \text{ m}^2 = 48 \text{ m}^2$

- 6. An umbrella is made by stitching 10 triangular pieces of cloth of two different colours (see Fig.12.16), each piece measuring 20 cm, 50 cm and 50 cm. How much cloth of each colour is required for the umbrella?**



Fig. 12.16

Solution:

For each triangular piece, The semi perimeter will be

$$s = (50 + 50 + 20)/2 \text{ cm} = 120/2 \text{ cm} = 60\text{cm}$$

Using Heron's formula,

$$\text{Area of the triangular piece} = \sqrt{[s (s-a) (s-b) (s-c)]}$$

$$= \sqrt{[60(60 - 50) (60 - 50) (60 - 20)] \text{ cm}^2}$$

$$= \sqrt{[60 \times 10 \times 10 \times 40] \text{ cm}^2}$$

$$= 200\sqrt{6} \text{ cm}^2$$

$$\therefore \text{The area of all the triangular pieces} = 5 \times 200\sqrt{6} \text{ cm}^2 = 1000\sqrt{6} \text{ cm}^2$$

